

From: [Perlner, Ray \(Fed\)](#)
To: [Alperin-Sheriff, Jacob \(Fed\)](#); [Peralta, Rene C. \(Fed\)](#); [Liu, Yi-Kai \(Fed\)](#); [Moody, Dustin \(Fed\)](#); [Bassham, Lawrence E. \(Fed\)](#); [Chen, Lily \(Fed\)](#); [Daniel Smith-Tone](#); [Jordan, Stephen P \(Fed\)](#); [Miller, Carl A. \(Fed\)](#); [Smith-Tone, Daniel C. \(Fed\)](#)
Subject: RE: Proposed edits to security strengths section
Date: Friday, October 7, 2016 5:24:00 PM

One additional note: (b) (6)

[REDACTED]

[REDACTED]

[REDACTED]

From: Perlner, Ray (Fed)
Sent: Friday, October 07, 2016 5:16 PM
To: Alperin-Sheriff, Jacob (Fed) <jacob.alperin-sheriff@nist.gov>; Peralta, Rene (Fed) <rene.peralta@nist.gov>; Liu, Yi-Kai (Fed) <yi-kai.liu@nist.gov>; Moody, Dustin (Fed) <dustin.moody@nist.gov>; Bassham, Lawrence E (Fed) <lawrence.bassham@nist.gov>; Chen, Lily (Fed) <lily.chen@nist.gov>; 'Daniel Smith-Tone' <daniel-c.smith@louisville.edu>; Jordan, Stephen P (Fed) <stephen.jordan@nist.gov>; Miller, Carl A. (Fed) <carl.miller@nist.gov>; Smith-Tone, Daniel (Fed) <daniel.smith@nist.gov>

Subject: RE: Proposed edits to security strengths section

Jacob suggested to me that what I currently have written may be ok if it's supplemented with a reference to translate between units of AES operations and basic bit operations.

I was able to find a decent reference for the complexity of Grover's algorithm on AES:

<https://arxiv.org/pdf/1512.04965v1.pdf>

This would suggest that an attack on AES with a maximum depth MAXDEPTH requires:

$2^{170/\text{MAXDEPTH}}$ for AES128 (up to $\text{MAXDEPTH}=2^81$)

$2^{233/\text{MAXDEPTH}}$ for AES192 (up to $\text{MAXDEPTH}=2^{113}$)

$2^{298/\text{MAXDEPTH}}$ for AES256 (up to $\text{MAXDEPTH}=2^{145}$)

(all measured based on total number of gates in the Clifford-T gate set.)

I wasn't able to find a comparable classical gate count for SHA2 or SHA3 (and I'm not sure that's the classical security metric Yi-Kai wants) but I'd guess total gate count for either compression function is somewhere around 2^{20} classical gates. This would suggest that, for any plausible value of

MAXDEPTH, Van Oorschot-Wiener parallel collision search requires a total of

2^{148} classical gates for SHA256/SHA3-256

2^{212} classical gates for SHA384/SHA3-384

(2^{276} classical gates for SHA512/SHA3-512)

As a side note, this would imply that, even ignoring the probability that quantum gates are more expensive than classical gates, security strengths 2 and 4 are less than security strengths 3 and 5 as long as $\text{MAXDEPTH} < 2^{85}$. (This is very close to the limit of what's possible with atomic scale qubits and speed of light propagation time.)

From: Perlner, Ray (Fed)
Sent: Friday, October 07, 2016 11:25 AM
To: Alperin-Sheriff, Jacob (Fed) <jacob.alperin-sheriff@nist.gov>; Peralta, Rene (Fed) <rene.peralta@nist.gov>; Liu, Yi-Kai (Fed) <yi-kai.liu@nist.gov>; Moody, Dustin (Fed) <dustin.moody@nist.gov>; Bassham, Lawrence E (Fed) <lawrence.bassham@nist.gov>; Chen, Lily (Fed) <lily.chen@nist.gov>; Daniel Smith-Tone <daniel-c.smith@louisville.edu>; Jordan, Stephen P

(Fed) <stephen.jordan@nist.gov>; Miller, Carl A. (Fed) <carl.miller@nist.gov>; Smith-Tone, Daniel (Fed) <daniel.smith@nist.gov>

Subject: RE: Proposed edits to security strengths section

True. I agree that we should have a "purely ephemeral only" KEM with IND-CPA security. Typically you still need symmetric crypto to get IND-CPA, though, so even there I think comparing security to that of symmetric primitives is unavoidable.

From: Alperin-Sheriff, Jacob (Fed)

Sent: Friday, October 07, 2016 11:19 AM

To: Perlner, Ray (Fed) <ray.perlner@nist.gov>; Peralta, Rene (Fed) <rene.peralta@nist.gov>; Liu, Yi-Kai (Fed) <yi-kai.liu@nist.gov>; Moody, Dustin (Fed) <dustin.moody@nist.gov>; Bassham, Lawrence E (Fed) <lawrence.bassham@nist.gov>; Chen, Lily (Fed) <lily.chen@nist.gov>; Daniel Smith-Tone <daniel-c.smith@louisville.edu>; Jordan, Stephen P (Fed) <stephen.jordan@nist.gov>; Miller, Carl A. (Fed) <carl.miller@nist.gov>; Smith-Tone, Daniel (Fed) <daniel.smith@nist.gov>

Subject: Re: Proposed edits to security strengths section

I'm still not entirely convinced that CCA security is required for fully ephemeral key exchange, though, as any information learned by a CCA-style attack on a single session will be useless for any other sessions. Since by other means (i.e the authentication aspect of the protocol), the CCA attack should only be mountable by Eve if Alice (or Bob) intended to start a session key exchange with Eve in the first place, a CCA-style attack is only going to potentially yield Eve information about Alice (or Bob)'s secret key information for that particular session, and it's of no concern if she learns that since she already knows everything that the secret key information is used for, namely deriving the session key.

I suppose this situation could be more easily screwed up by cryptographically less-than-knowledgeable implementers, more so than if it had the additional CCA security, but I can't think of any other reason to require CCA for fully ephemeral exchange.

From: "Perlner, Ray (Fed)" <ray.perlner@nist.gov>

Date: Friday, October 7, 2016 at 10:19 AM

To: "Alperin-Sheriff, Jacob M. (Fed)" <jacob.alperin-sheriff@nist.gov>, "Peralta, Rene (Fed)" <rene.peralta@nist.gov>, "Liu, Yi-Kai (Fed)" <yi-kai.liu@nist.gov>, "Moody, Dustin (Fed)" <dustin.moody@nist.gov>, "Bassham, Lawrence E (Fed)" <lawrence.bassham@nist.gov>, "Chen, Lily (Fed)" <lily.chen@nist.gov>, Daniel Smith-Tone <daniel-c.smith@louisville.edu>, "Jordan, Stephen P (Fed)" <stephen.jordan@nist.gov>, "Miller, Carl A. (Fed)" <carl.miller@nist.gov>, "Smith-Tone, Daniel (Fed)" <daniel.smith@nist.gov>

Subject: RE: Proposed edits to security strengths section

I strongly disagree that the definition comparing security to AES/SHA3 is harder to use than one that specifies concrete numbers in terms of a gate set

- 1) What we're standardizing are modes that provide CCA/CMA security. This almost certainly means that block ciphers or hash functions will be used in the padding and/or in the message representative. So, cryptanalysts cannot avoid thinking about the cost of attacking a block cipher or hash function.
- 2) The natural units for a lot of cryptanalytic attacks are not basic machine instructions or gates in the first place. Rather, it is very common to think in terms of field or matrix operations, which are not much easier to analyze than AES in terms of basic gates or real machines. And, unlike standard symmetric crypto primitives, you're less likely to find someone who went to the effort to create a genuinely optimized implementation, especially if the field/matrix size

is not a round number.

- 3) Classical cryptanalysis needs to remain a big part of our evaluation, since, if the best theoretical attack is a variant of Grover's algorithm, there's a significant chance that the best attack in practice will simply be the classical attack. Specifying everything in terms of gate sets etc. will be incomprehensible to people used to doing classical cryptanalysis. The literature in classical cryptanalysis almost exclusively gives estimates in bits of security. Granted, the unit of work isn't always explicitly an AES operation. Cryptanalysts are happy enough to consider an AES operation, a SHA compression function, a modular multiplication over thousand bit integers etc. to be "about the same amount of work" because they really don't care whether something has 80 bits of security, 75 or 87. If you're cutting your security margin close enough that a few bits of security matter, you're probably cutting it too close. I think this goes double for our process, since the best attacks on asymmetric primitives have a habit of moving significantly.

Regarding Yi-Kai's last suggesting about measuring the "real world" cost of classical and quantum attacks. I believe that is what my currently proposed text is doing. The 5 security categories are merely meant as landmarks along the way so that we can compare like with like when doing performance comparisons, and so that cryptanalysts can be free to choose their own security metric without making their attacks completely incommensurable with every other piece of research out there.

From: Alperin-Sheriff, Jacob (Fed)

Sent: Thursday, October 06, 2016 2:31 PM

To: Peralta, Rene (Fed) <rene.peralta@nist.gov>; Liu, Yi-Kai (Fed) <yi-kai.liu@nist.gov>; Perlner, Ray (Fed) <ray.perlner@nist.gov>; Moody, Dustin (Fed) <dustin.moody@nist.gov>; Bassham, Lawrence E (Fed) <lawrence.bassham@nist.gov>; Chen, Lily (Fed) <lily.chen@nist.gov>; Daniel Smith-Tone <daniel-c.smith@louisville.edu>; Jordan, Stephen P (Fed) <stephen.jordan@nist.gov>; Miller, Carl A. (Fed) <carl.miller@nist.gov>; Smith-Tone, Daniel (Fed) <daniel.smith@nist.gov>

Subject: Re: Proposed edits to security strengths section

I wasn't going to heavily rock the boat (although I did ask about it), but that was also the main weird issue I had when I first read the draft proposal myself when I started here ...

From: "Peralta, Rene (Fed)" <rene.peralta@nist.gov>

Date: Thursday, October 6, 2016 at 2:29 PM

To: "Liu, Yi-Kai (Fed)" <yi-kai.liu@nist.gov>, "Perlner, Ray (Fed)" <ray.perlner@nist.gov>, "Moody, Dustin (Fed)" <dustin.moody@nist.gov>, "Alperin-Sheriff, Jacob M. (Fed)" <jacob.alperin-sheriff@nist.gov>, "Bassham, Lawrence E (Fed)" <lawrence.bassham@nist.gov>, "Chen, Lily (Fed)" <lily.chen@nist.gov>, Daniel Smith-Tone <daniel-c.smith@louisville.edu>, "Jordan, Stephen P (Fed)" <stephen.jordan@nist.gov>, "Miller, Carl A. (Fed)" <carl.miller@nist.gov>, "Smith-Tone, Daniel (Fed)" <daniel.smith@nist.gov>

Cc: "Peralta, Rene (Fed)" <rene.peralta@nist.gov>

Subject: Re: Proposed edits to security strengths section

I tend to agree with Yi-Kai. If we are concerned about some sort of common complexity measure with other NIST standards, maybe we can look into that as a separate item as this project progresses.

Rene.

From: Liu, Yi-Kai (Fed)

Sent: Thursday, October 6, 2016 12:02 PM

To: Perlner, Ray (Fed); Moody, Dustin (Fed); Alperin-Sheriff, Jacob (Fed); Bassham, Lawrence E (Fed); Chen, Lily (Fed); Daniel Smith-Tone; Jordan, Stephen P (Fed); Miller, Carl A. (Fed); Peralta, Rene (Fed); Smith-Tone, Daniel (Fed)

Subject: Re: Proposed edits to security strengths section

Thanks Ray! I've been thinking about this, however, and I am becoming more and more convinced that it is a bad idea to define our security levels for PQC in terms of the resources needed to break block ciphers and hash functions. I have two objections:

1. This definition is hard for cryptanalysts to use, because it forces them to convert their results from natural units (e.g., number of arithmetic operations, number of gates, circuit depth) to unnatural ones (e.g., the amount of computational effort needed to break AES or SHA-3).
2. This definition is our way of ducking an important question: how much security do we want for PQC? A proper answer to that question would be something like "at least 2^{128} basic operations on a classical PRAM machine with 64-bit registers, and at least 2^{64} quantum gates over the basis {CNOT, Hadamard, Phase, $\pi/8$ }." Instead, we are telling the community we want "as much security as certain instantiations of AES and SHA-3," which is unhelpful, because they then have to go figure that out themselves (which is not easy).

Instead, I would favor a different approach:

1. I would much rather we specify some concrete security levels, in terms of some explicit models of computation. This will remove a lot of uncertainty in evaluating the complexity of cryptanalytic attacks. After seeing the public comments, I think this is a significant concern, and it has the potential to turn into a huge source of confusion when we start to evaluate the security of the different cryptosystems.
2. I think it is fine if the PQC security levels don't match the security of AES or SHA-3, because that is comparing apples and oranges anyway. I see this as a less serious problem than having a community-wide meltdown during the PQC competition.
3. Finally, I would suggest that maybe AES and SHA-3 are *not* good guides for the amount of quantum security we want for PQC. Mathematically, there is no reason why we should force the quantum security of PQC to behave the same way as it does for a hash function or block cipher. Instead, perhaps we should think about the "real world" cost of quantum versus classical attacks, and use THAT as the guide for how much quantum security we want for PQC.

Cheers, and sorry for the long email!

--Yi-Kai

From: Perlner, Ray (Fed)

Sent: Wednesday, October 5, 2016 12:20:03 PM

To: Moody, Dustin (Fed); Alperin-Sheriff, Jacob (Fed); Bassham, Lawrence E (Fed); Chen, Lily (Fed); Daniel Smith-Tone; Jordan, Stephen P (Fed); Liu, Yi-Kai (Fed); Miller, Carl A. (Fed); Peralta, Rene (Fed); Smith-Tone, Daniel (Fed)

Subject: Proposed edits to security strengths section

Since I will be gone for the next PQC meeting, Dustin asked me to try rewriting the security strengths section (which I have now divided into 4.A.4 and 4.A.5) See attached

Thanks,

Ray